

Probability midterm exam (Model 2)

Question (1):

(A) A card is drawn at random variable from an ordinary deck of 52 playing cards. Find the probability that it is (a) Ace (b) A jack of hearts (c) A three of club or six of diamonds (d) A hearts (e) Any suit except hearts (f) A ten or speeds (g) Neither a four nor a club?

(B) Four different mathematics books, six different physics books, and two different chemistry books are to be arranged on a shelf. How many different arrangements are possible if (a) The books in each subject must all stand together, (b) Only the mathematics books must stand together?

Question (2):

The joint density function of two discrete random variable X and Y is given by $f(x,y)=c(2x+y)$, where x and y can assume all integers such that $0 \leq x \leq 2$, $0 \leq y \leq 3$ and $f(x,y)=0$ otherwise.

(a) Find the value of constant C .

(b) Find $P(X \geq 1, Y \leq 2)$.

(c) Find $P(X=2, Y=1)$.

(d) Find the marginal probability function of X .

(e) Find the marginal probability function of Y .

(f) Show that random variables X and Y are dependent.

Question (3):

If $X^* = (X - \mu) / \delta$ is a standardized random variable, Prove that (a) $E(X^*) = 0$, (b) $\text{Var}(X^*) = 1$?